

Non-monotonic Relaxation Kinetics of Confined Systems



Yaroslav Ryabov

University of Maryland

Alexander Puzenko

Yuri Feldman

Hebrew University of Jerusalem

Phys Rev B, **69** 014204 (2004)

Kinetics Models

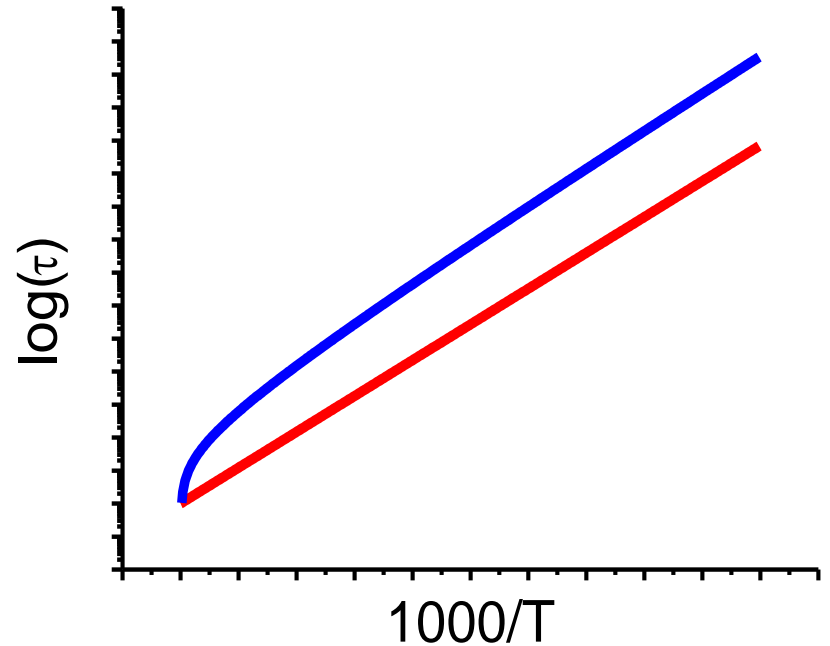
Transition state theory

Arrhenius Law (1889)

$$\tau = \tau_0 \exp\left(\frac{E_a}{kT}\right)$$

Eyring Law (1935)

$$\tau = \frac{h}{kT} \exp\left(\frac{\Delta H}{kT} - \frac{\Delta S}{k}\right)$$



Kinetics Models

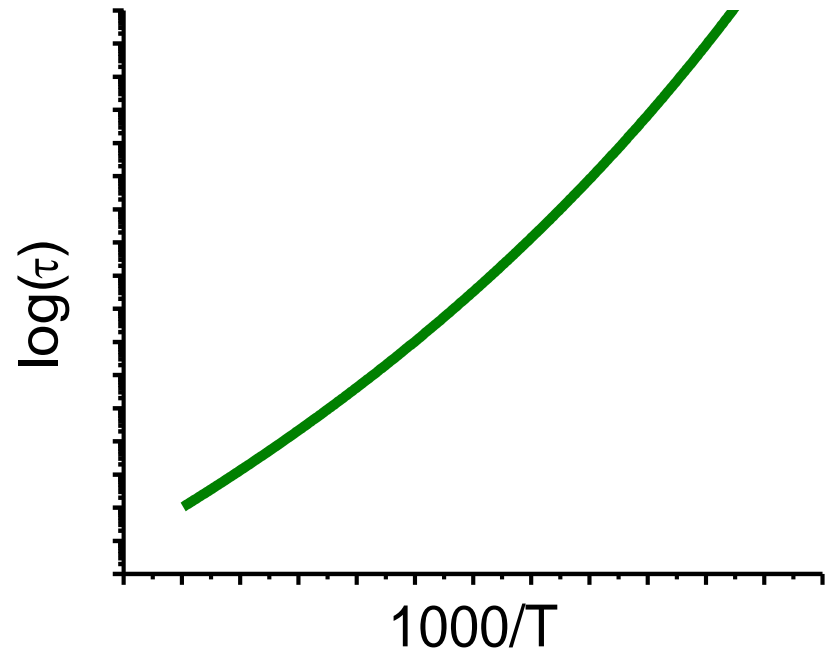
Free Volume concept

Vogel-Fulcher-Tamman VFT (1921,1925,1926)

$$\tau = \tau_0 \exp\left(\frac{DT_k}{T - T_k}\right)$$

$$\tau = \tau_0 \exp\left(\frac{V_0}{V_F}\right)$$

$$V_F \sim T - T_k$$



Fox and Flory (1950)

Adam and Gibbs (1965)

Kinetics Models

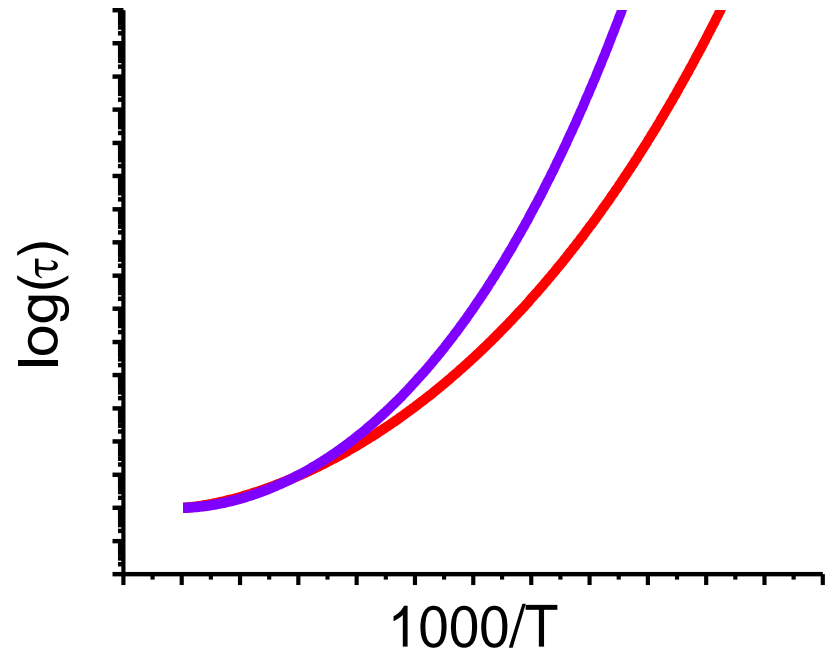
**Bendler and
Shlesinger (1987)**
Mobile defects in amorphous state

$$\tau = \tau_0 \exp\left(\frac{B}{(T - T_K)^{3/2}}\right)$$

**Bengtzelius,
Götze and Sjölander (1984)**
MCT

$$\tau = \tau_0 \exp\left(\frac{F}{(T - T_K)^\gamma}\right)$$

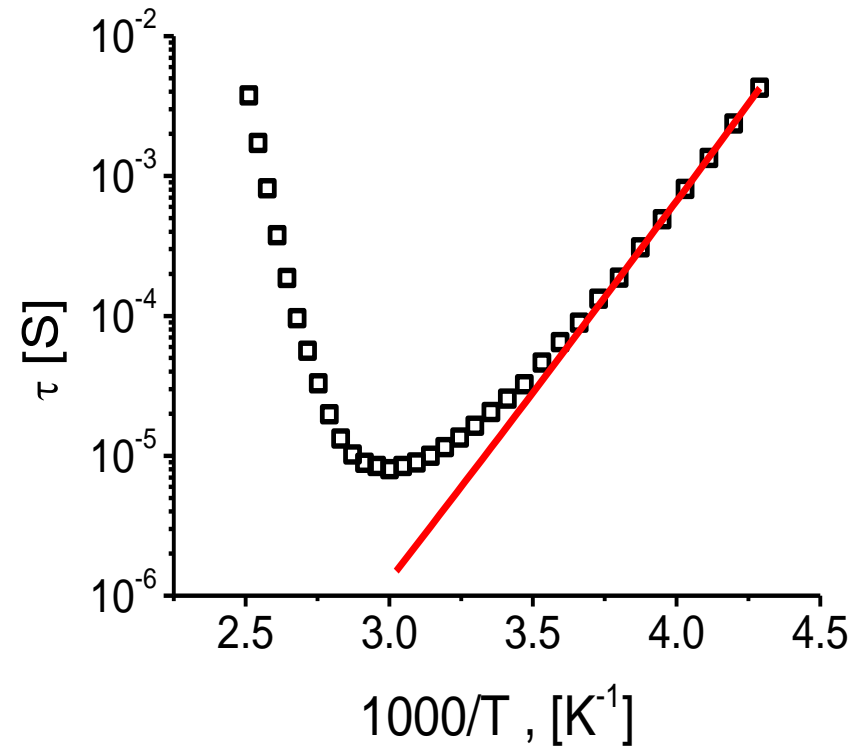
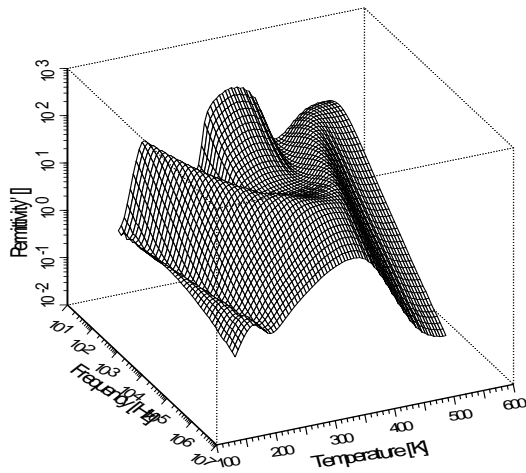
$$\gamma \approx 1.76$$



Non-monotonic Kinetics

Experimental observations

**Water confined
in a porous glass sample
Gutina et al. (1998)**



Non-monotonic Kinetics

The Model

$$\frac{1}{\tau} \sim p_1 p_2 \quad p_1 = \exp\left(-\frac{E_a}{kT}\right) \quad p_2 = \exp\left(-\frac{V_0}{V_F}\right)$$

Number of active particles

$$n = n_0 \exp\left(-\frac{E_b}{kT}\right)$$

Free Volume per particle

$$\frac{1}{V_F} \sim n_0 \exp\left(-\frac{E_b}{kT}\right)$$

Total volume of the system

$$V = \text{const}$$

$$\tau = \tau_0 \exp\left\{\frac{E_a}{kT} + \frac{V_0 n_0}{V} \exp\left(-\frac{E_b}{kT}\right)\right\}$$

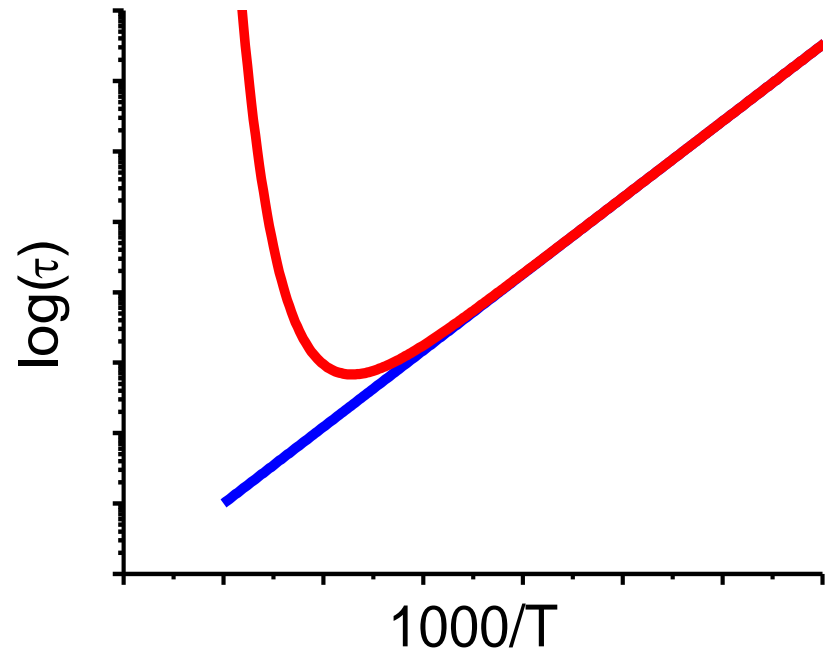
Non-monotonic Kinetics

The Model

$$\tau = \tau_0 \exp \left\{ \frac{E_a}{kT} + \frac{V_0 n_0}{V} \exp \left(-\frac{E_b}{kT} \right) \right\}$$

$$n_0 \ll \frac{V}{V_0} \quad \text{Unconfined system with Arrhenius kinetics}$$

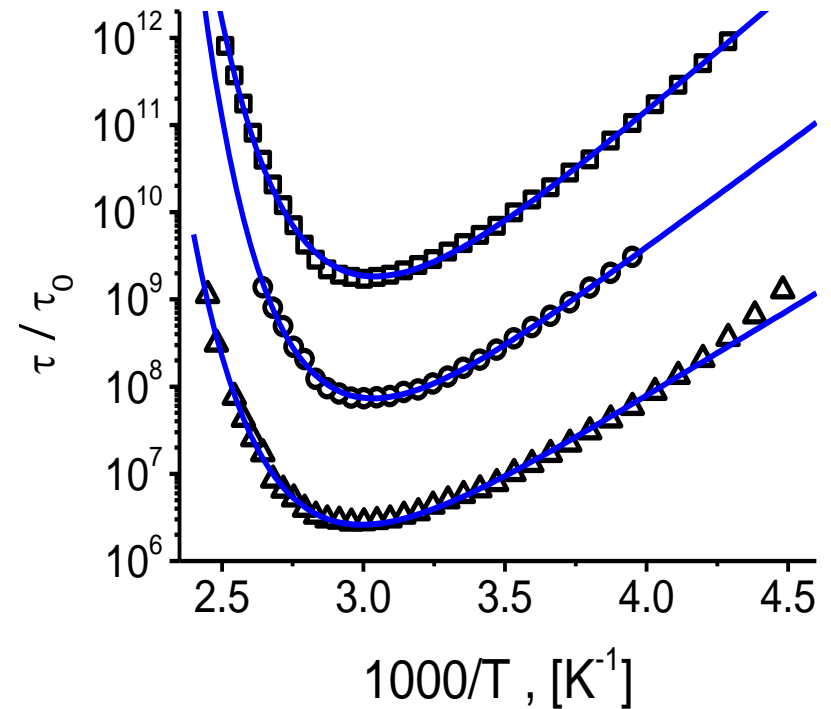
$$n_0 \gg \frac{V}{V_0} \quad \text{Confined system with non-monotonies kinetics}$$



Model VS Experiment

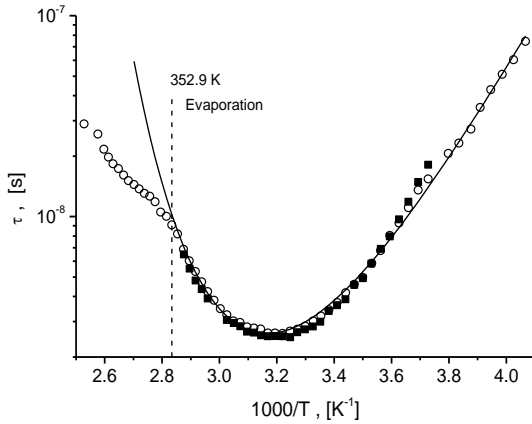
Water confined in Porous Glasses

Sample	E_a [kJ/mol]	E_b [kJ/mol]	$n_0 V_\sigma/V$	$\text{Ln } \tau_0$
A ○	46	33	27×10^4	-27
B □	53	29	7×10^4	-33
C △	38	32	12×10^4	-26



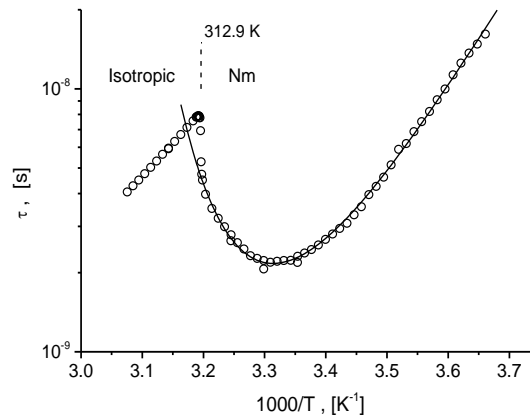
Model VS Experiment

Water in Zeolites



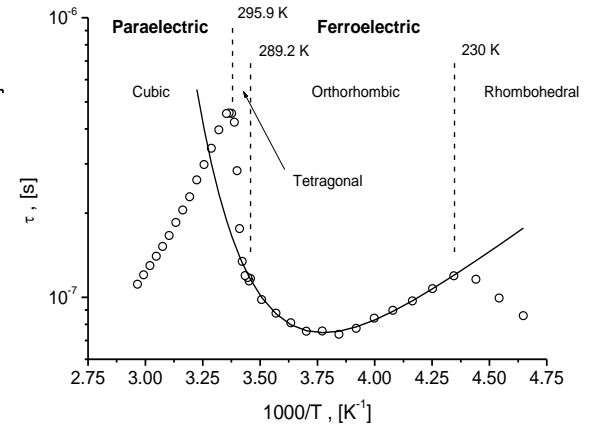
Schönhals et al. (2002)

Confined 8CB liquid crystal



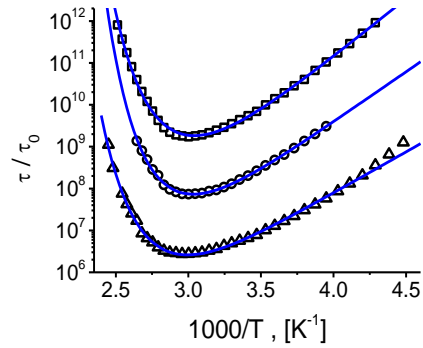
Aliev et al. (2002)

KTN ferroelectric crystal



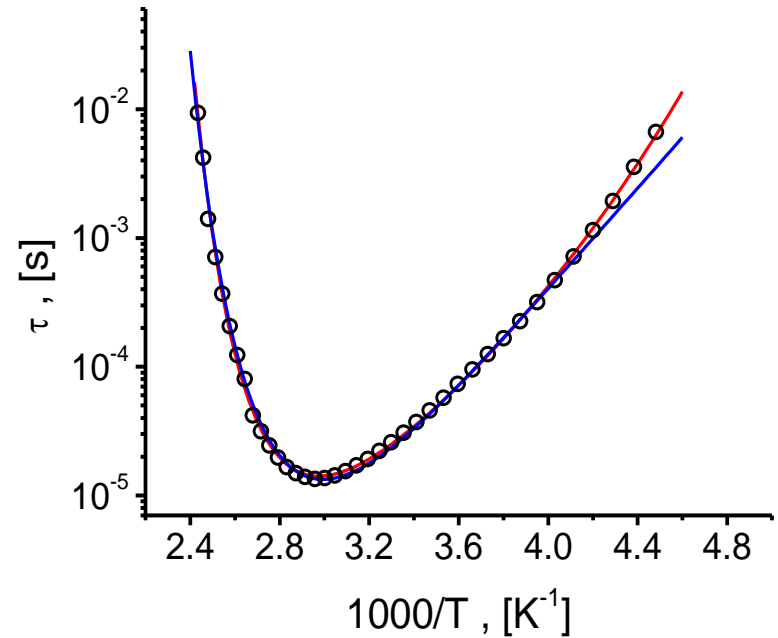
Feldman et al. (2004, 2005)

Confined Supercooled Water



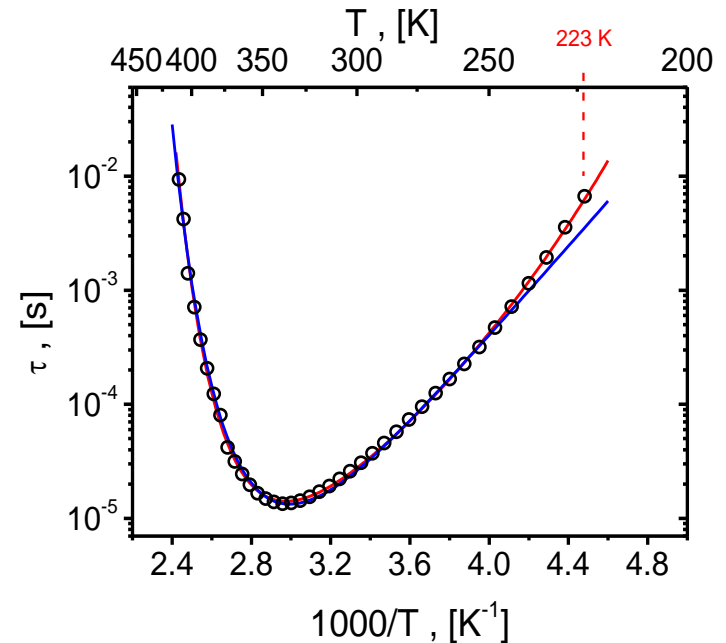
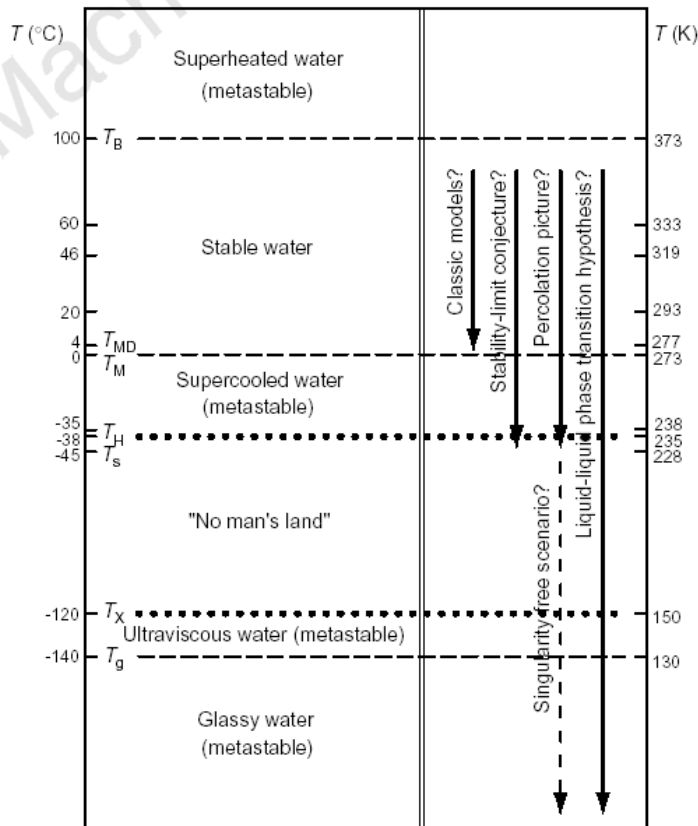
$$p_1 = \exp\left(-\frac{DT_k}{T - T_k}\right)$$

$$\tau = \tau_0 \exp\left\{\frac{DT_k}{T - T_k} + \frac{V_0 n_0}{V} \exp\left(-\frac{E_b}{kT}\right)\right\}$$



Confined Supercooled Water

Mishima and Stanley (1998)



$$T_k = 124 \pm 7 \text{ [K]} \quad D = 10 \pm 2$$

$$T_g \sim 140 \text{ [K]} \quad D \sim 8$$

Johary et al. (1987),
Smith and Kay (1999)

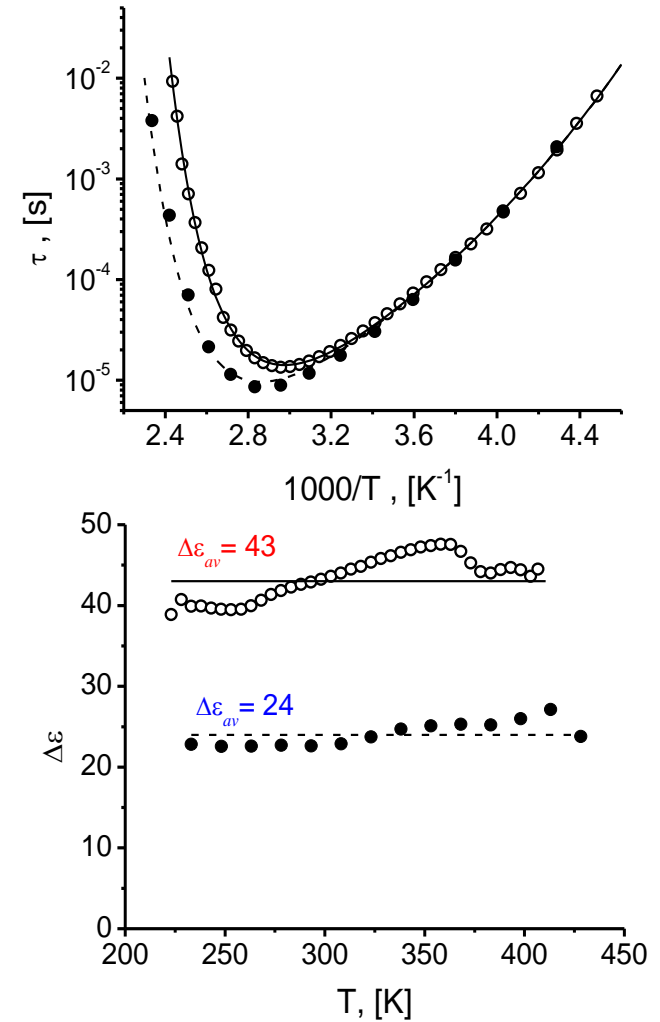
Confinement Factor

$$\tau = \tau_0 \exp \left\{ \frac{DT_k}{T - T_k} + \frac{V_0 n_0}{V} \exp \left(- \frac{E_b}{kT} \right) \right\}$$

$$\frac{V_0 n_0}{V}$$

$$n_0 \sim \Delta \varepsilon$$

$$\frac{\Delta \varepsilon_{av}}{\Delta \varepsilon} = 1.8$$



Protein folding kinetics

Random Energy Model

Derrida (1980)

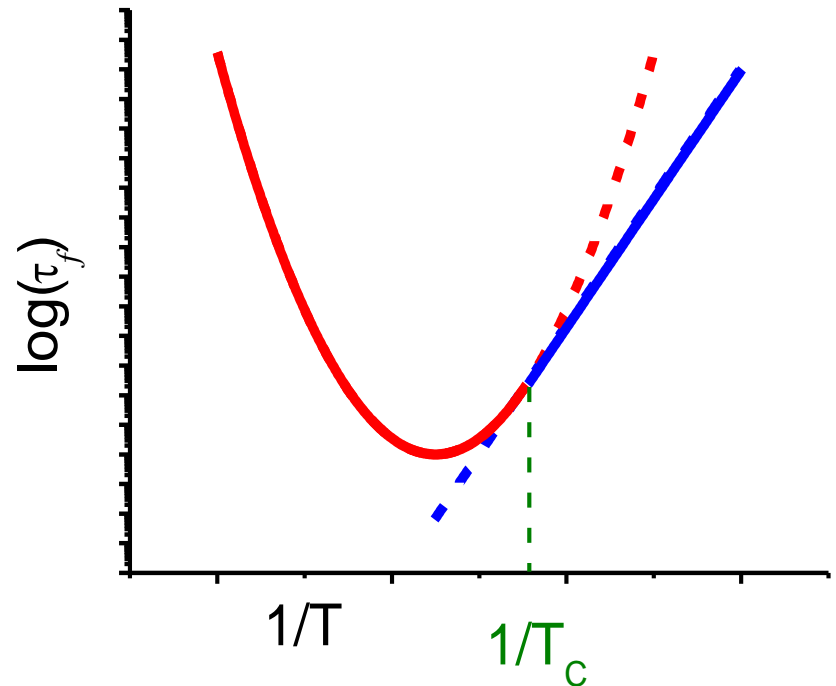
$$n(E) = \frac{\Omega}{\sqrt{2\pi\Sigma^2}} \exp\left(-\frac{(E - \bar{E})^2}{2\Sigma^2}\right)$$

Bryngelson and Wolynes (1987, 1989)

$$\ln\left(\frac{\tau_f}{\tau_0}\right) = \frac{E^*}{kT} + \frac{E_c T_c}{2k^2} \left(\frac{1}{T} - \frac{1}{T_c}\right)^2 \quad T > T_c$$

$$\ln\left(\frac{\tau_f}{\tau_0}\right) = \frac{E^*}{kT} \quad T < T_c$$

$$E_c = \bar{E} - \Sigma\sqrt{1\ln\Omega}$$



Protein folding kinetics

Confinement in Conformation space

$$p_f = p_b^q p_n^{qN}$$

Probability to have
an 'active' bond

$$p_b = \exp\left(-\frac{E_b}{kT}\right)$$

Probability to find
an 'proper' connection

$$p_n = \exp\left(-\frac{\omega_0}{\omega_f}\right)$$

Total conformation volume

$$\Omega_0 = q^N$$

Free conformation volume

$$\omega_f = \frac{\Omega_0}{N_d}$$

$$\omega_0 = \frac{\Omega_0}{qN}$$

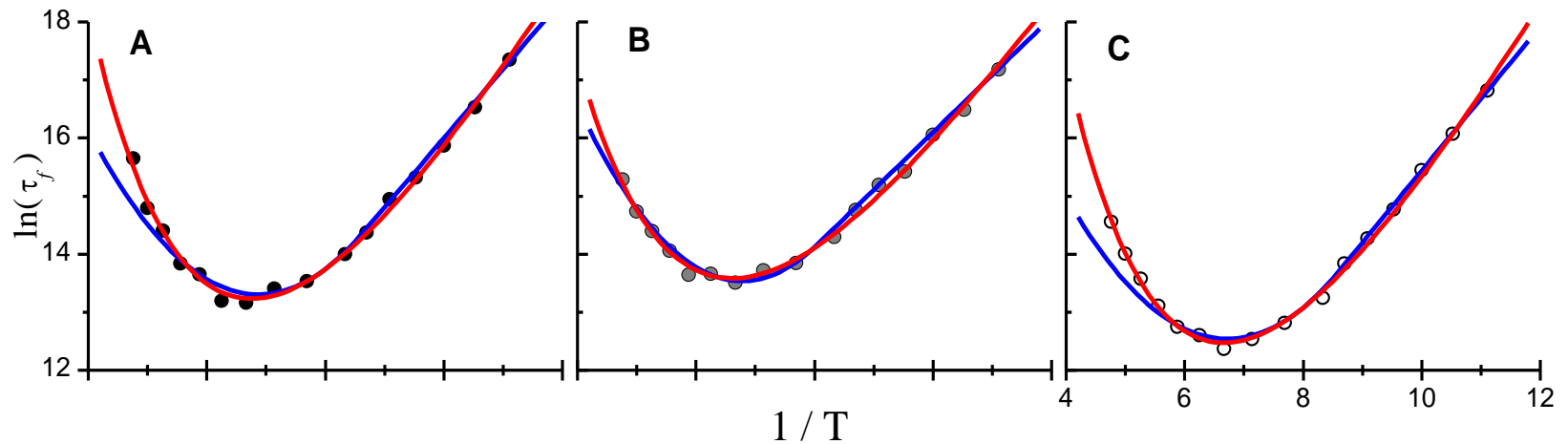
$$\omega_f = qN \exp\left(\frac{E_b}{kT}\right)$$

$$\tau_f \sim \frac{1}{p_f} \sim q \frac{E_b}{kT} + qN \exp\left(-\frac{E_b}{kT}\right)$$

Protein folding kinetics

Models VS simulation data

Simulation data from Shakhovich et al. 1998



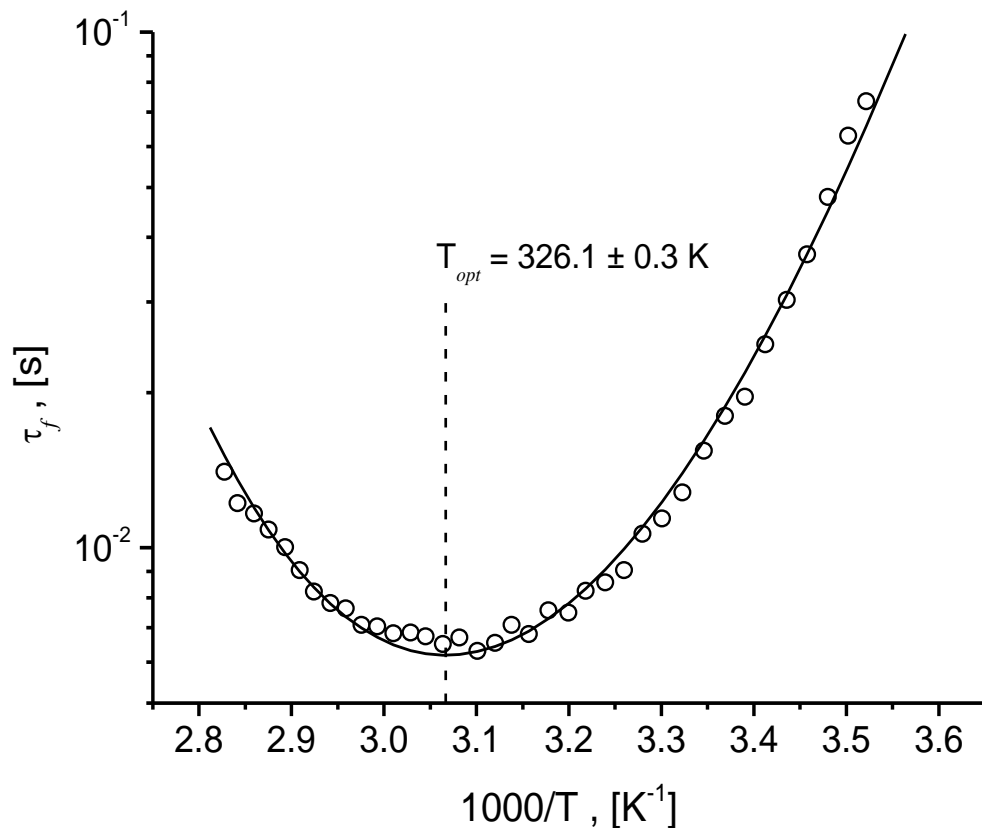
$N = 27$

	REM					Confinement Model			
	$\ln \tau_0$	E_c	E^*	$1/T_C$	χ^2	$\ln \tau_0$	E_b	q	χ^2
A	4.20	-5.92	1.19	8.60	0.077	-1.18	0.49	3.26	0.010
B	6.10	-6.32	0.99	58.04	0.016	1.84	0.50	2.73	0.008
C	3.04	-5.68	1.24	8.60	0.083	2.14	0.49	3.40	0.006

Protein folding kinetics

Model VS experimental data

Data from Fersht et al. 1996 (CI2)



$$\ln \tau_0 = -83$$

$$E_b = 11.3$$

$$qN = 967$$

**More experimental
data needed**

Protein folding kinetics

Levintahal's Paradox (1969)

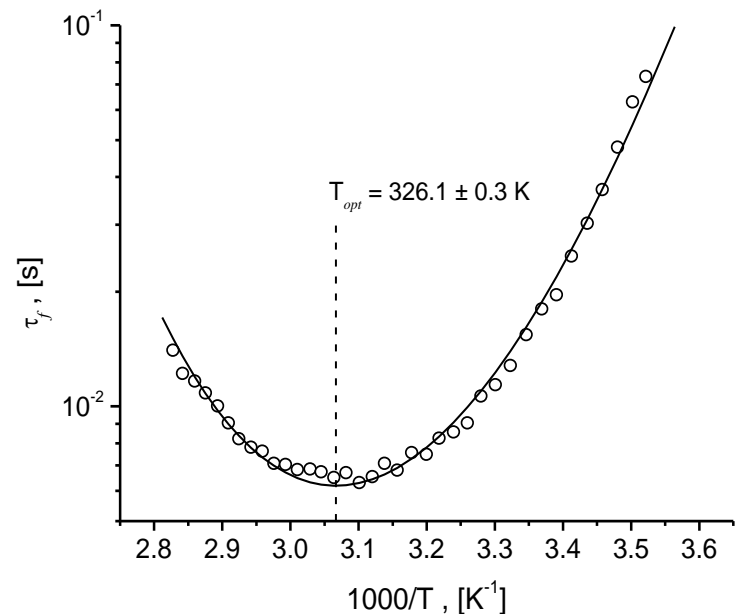
$$\tau_f = \tau_0 q^N$$

Algebraic scaling

$$\tau_{fast} = \tau_0 (eN)^q$$

$$q \sim 2 \div 3$$

Camacho and Thirumalai (1993)



Have To be tested

$$T_{opt} = \frac{E_b}{k \ln N}$$

Conclusions



- **Non monotonous kinetics can be a result of confinement either in real or in conformational space**
- ✓ **Confined water can be supercooled below its homogeneous nucleation point which opens new possibilities for investigation of water glass state**
- ✓ **The concept of confinement in conformational space can serve as a paradigm for protein folding kinetics, which leads to known algebraic scaling for protein folding times.**

Thanks



Yuri Feldman

Alexander Puzenko

Anna Gutina

Fouad Aliev

Andreas Schönhals

HUJI

And You